

COMP 122/L
Summer 2023

Karnaugh Maps (K-Maps) (Answers)

For each truth table, you must first write the table in an equivalent sum-of-products formula. From there, you'll need to write out a K-map, draw boxes as appropriate, and write out the equivalent optimized sum-of-products formula.

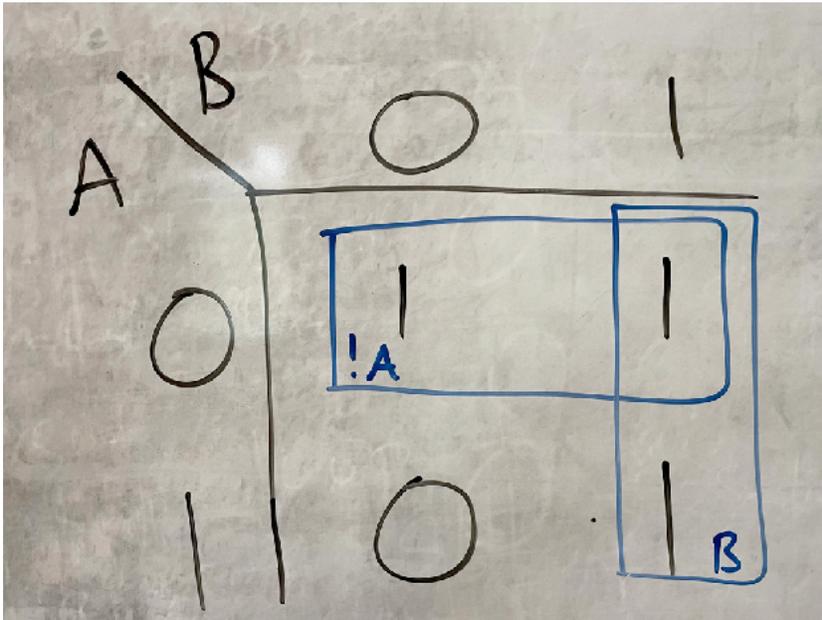
1.)

A	B	Output
0	0	1
0	1	1
1	0	0
1	1	1

1.a.) As an unoptimized sum-of-products formula:

$$\text{Output} = !A!B + !AB + AB$$

1.b.) As a K-map:



1.c.) As an optimized sum-of-products formula:

$$\text{Output} = !A + B$$

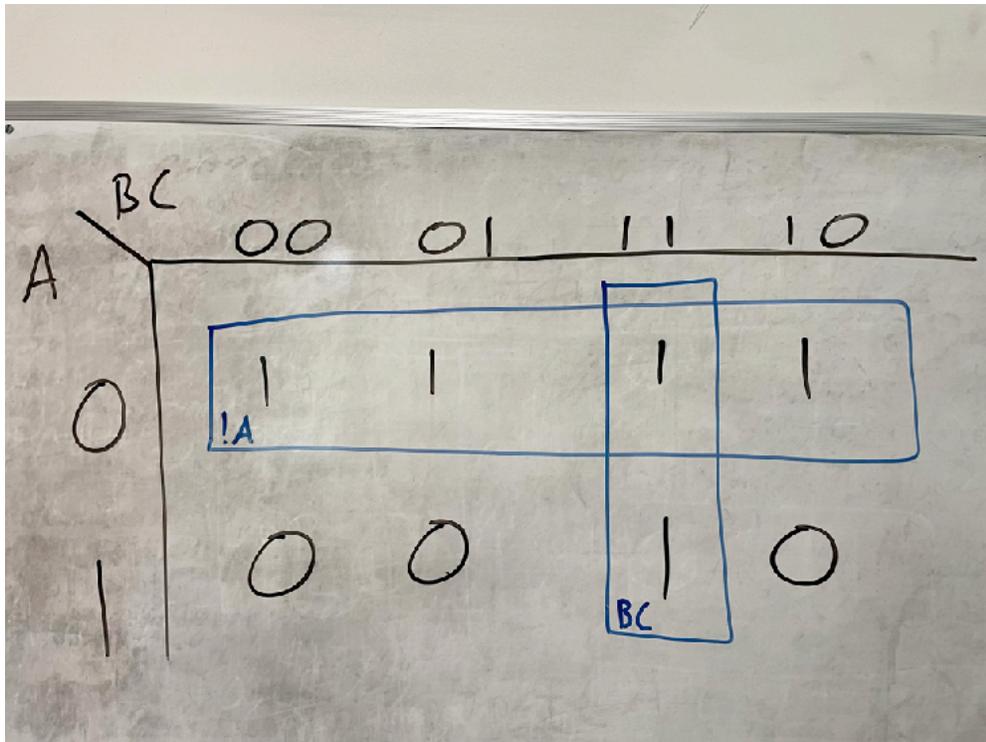
2.)

A	B	C	Output
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

2.a.) As an unoptimized sum-of-products formula:

$$\text{Output} = \neg A \neg B \neg C + \neg A \neg B C + \neg A B \neg C + \neg A B C + A \neg B \neg C + A \neg B C + A B \neg C + A B C$$

2.b.) As a K-map:



2.c.) As an optimized sum-of-products formula:

$$\text{Output} = \neg A + BC$$

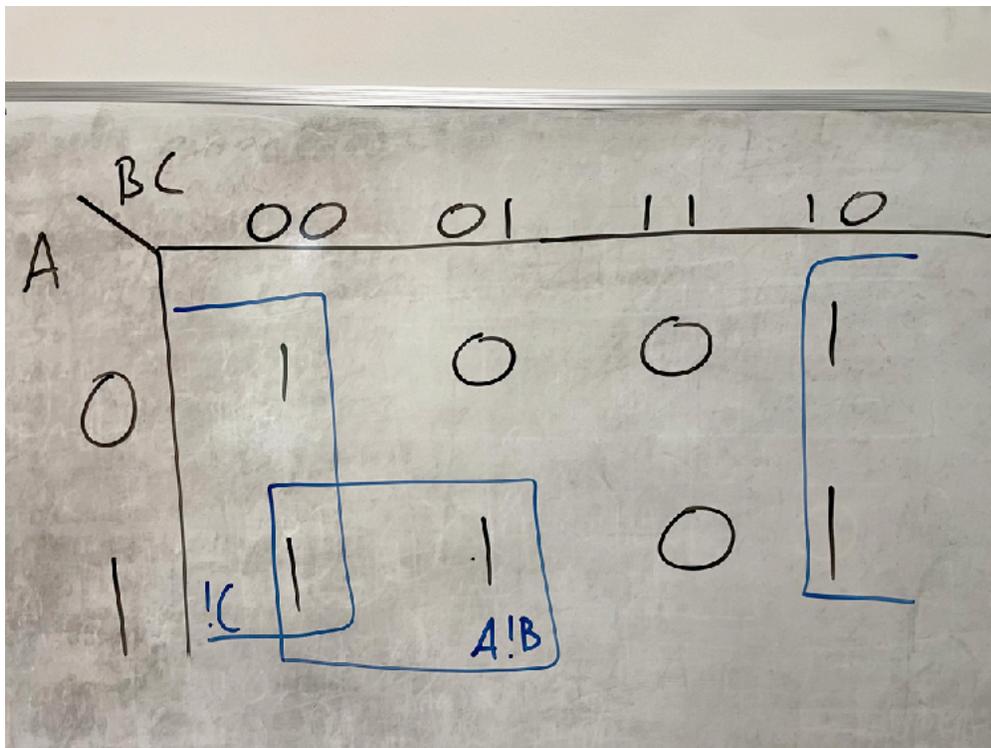
3.)

A	B	C	Output
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	1
1	1	1	1
1	1	1	0

3.a.) As an unoptimized sum-of-products formula:

$$\text{Output} = \neg A \neg B \neg C + \neg A \neg B C + A \neg B \neg C + A \neg B C + AB \neg C$$

3.b.) As a K-map:



3.c.) As an optimized sum-of-products formula:

$$\text{Output} = \neg C + A \neg B$$

4.)

A	B	C	D	Output
0	0	0	0	1
0	0	0	1	1
0	0	1	0	0
0	0	1	1	0
0	1	0	0	1
0	1	0	1	1
0	1	1	0	0
0	1	1	1	0
1	0	0	0	1
1	0	0	1	1
1	0	1	0	0
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	0
1	1	1	1	1

4.a.) As an unoptimized sum-of-products formula:

$$\begin{aligned} \text{Output} = & !A!B!C!D + !A!B!CD + \\ & !AB!C!D + !AB!CD + \\ & A!B!C!D + A!B!CD + \\ & A!BCD + AB!C!D + \\ & AB!CD + ABCD \end{aligned}$$

4.b.) As a K-map:

		CD			
		00	01	11	10
AB	00	1	1	0	0
	01	1	1	0	0
	11	1	1	1	0
	10	1	1	1	0

4.c.) As an optimized sum-of-products formula:

$$\text{Output} = !C + AD$$

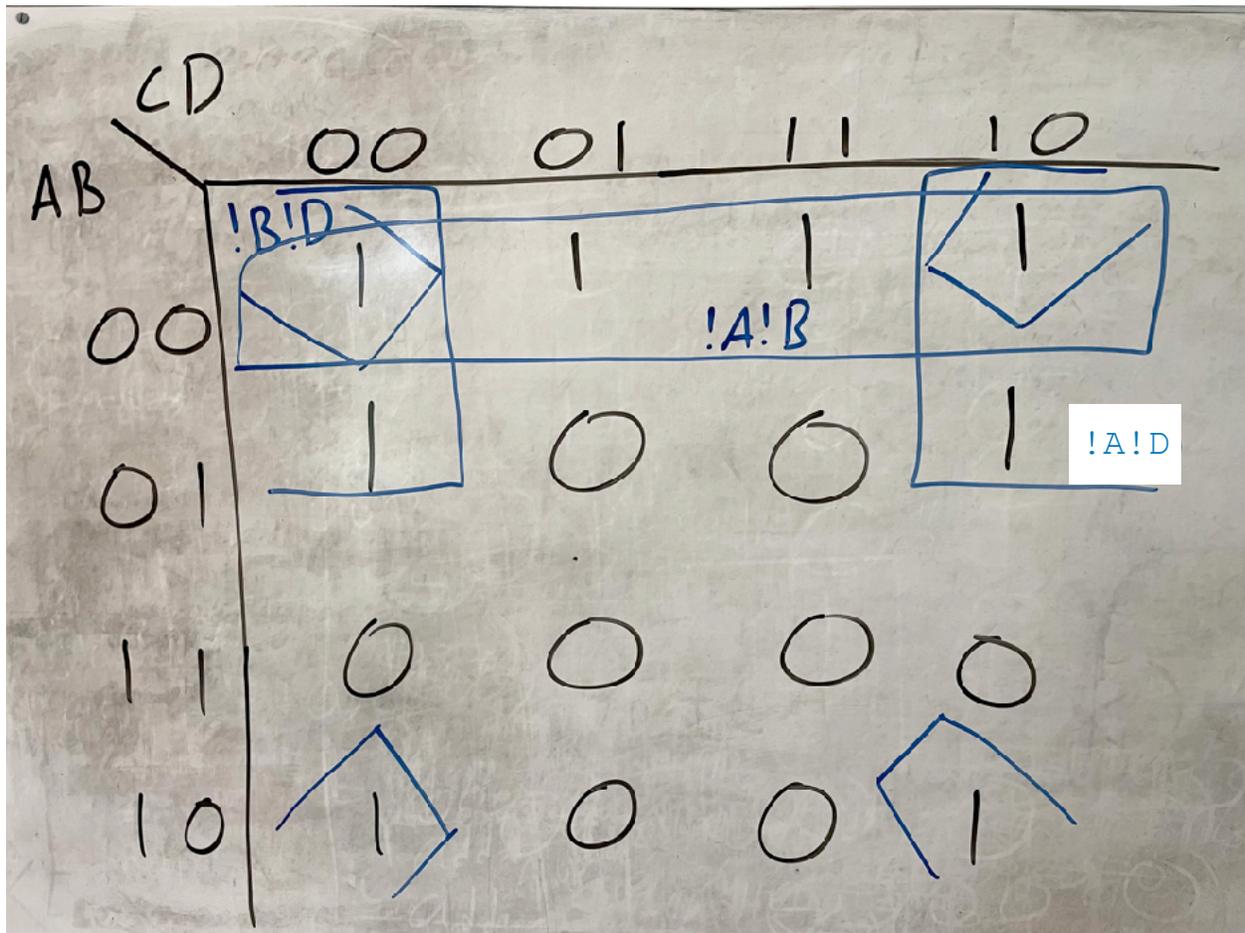
5.)

A	B	C	D	Output
0	0	0	0	1
0	0	0	1	1
0	0	1	0	1
0	0	1	1	1
0	1	0	0	1
0	1	0	1	0
0	1	1	0	1
0	1	1	1	0
1	0	0	0	1
1	0	0	1	0
1	0	1	0	1
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0
1	1	1	1	0

5.a.) As an unoptimized sum-of-products formula:

$$\begin{aligned} \text{Output} = & !A!B!C!D + !A!B!CD + \\ & !A!BC!D + !A!BCD + \\ & !AB!C!D + !AB!CD + \\ & A!B!C!D + A!BC!D \end{aligned}$$

5.b.) As a K-map:



5.c.) As an optimized sum-of-products formula:

$$\text{Output} = \overline{B}\overline{D} + \overline{A}\overline{B} + \overline{A}\overline{D}$$